

An Event Calculus for Run-Time Reasoning

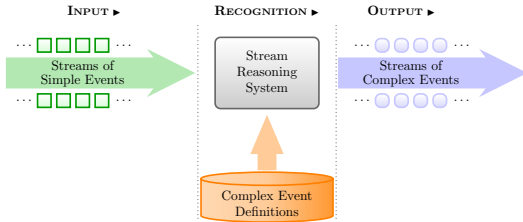
Periklis Mantenoglou

NCSR Demokritos, Greece
National and Kapodistrian University of Athens, Greece

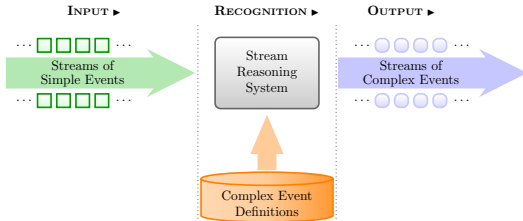
<http://cer.iit.demokritos.gr/>



Stream Reasoning



Stream Reasoning



[https://cer.iit.demokritos.gr \(maritime\)](https://cer.iit.demokritos.gr (maritime))

Event Calculus

- A **logic programming language** for representing and reasoning about events and their effects.
- Key components:
 - **event** (typically instantaneous).
 - **fluent**: a property that may have different values at different points in time.

Event Calculus

- A **logic programming language** for representing and reasoning about events and their effects.
- Key components:
 - **event** (typically instantaneous).
 - **fluent**: a property that may have different values at different points in time.
- Built-in representation of **inertia**:
 - $F = V$ holds at a particular time-point if $F = V$ has been *initiated* by an event at some earlier time-point, and not *terminated* by another event in the meantime.

Run-Time Event Calculus (RTEC): Fluent Specification

Simple Fluents:

initiatedAt($F = V, T$) \leftarrow
happensAt(E_{In_I}, T)[,
conditions].

\vdots

terminatedAt($F = V, T$) \leftarrow
happensAt(E_{T_I}, T)[,
conditions].

\vdots

where conditions:

$0-K$ [not] **happensAt**(E_k, T),

$0-M$ [not] **holdsAt**($F_m = V_m, T$),

$0-N$ atemporal-constraint_n

Run-Time Event Calculus (RTEC): Fluent Specification

Simple Fluents:

initiatedAt($F = V, T$) \leftarrow
happensAt($E_{I_{n1}}, T$)[,
conditions].

\vdots

terminatedAt($F = V, T$) \leftarrow
happensAt(E_{T_1}, T)[,
conditions].

\vdots

where conditions:

$0-K$ [not] **happensAt**(E_k, T),

$0-M$ [not] **holdsAt**($F_m = V_m, T$),

$0-N$ atemporal-constraint_n

Statically Determined Fluents:

holdsFor($F = V, I$) \leftarrow
holdsFor($F_1 = V_1, I_1$)[,
holdsFor($F_2 = V_2, I_2$), ...
holdsFor($F_n = V_n, I_n$),
intervalOperation(L_1, I_{n+1}), ...
intervalOperation(L_m, I)].

where intervalOperation:

union_all or

intersect_all or

relative_complement_all

Simple Fluent: High Speed Near Coast

initiatedAt(*highSpeedNC(Vessel) = true, T*) ←
happensAt(*velocity(Vessel, Speed, _CoG, _TrueHeading), T*),
holdsAt(*withinArea(Vessel, nearCoast) = true, T*),
threshold(v_{hs}, V), Speed > V).

Simple Fluent: High Speed Near Coast

initiatedAt($highSpeedNC(Vessel) = true, T$) \leftarrow
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terminatedAt($highSpeedNC(Vessel) = true, T$) \leftarrow
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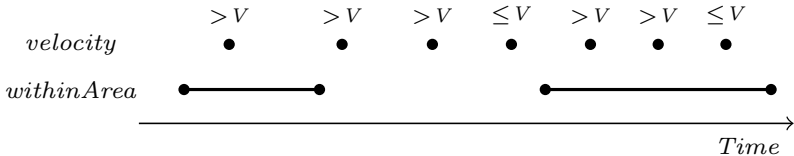
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Reasoning: **holdsFor**($highSpeedNC(Vessel) = true, I$)



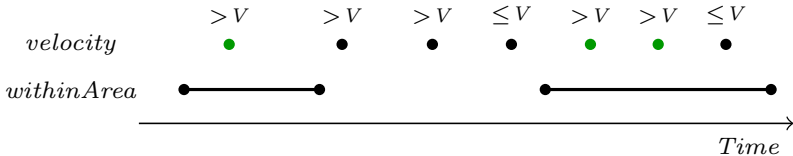
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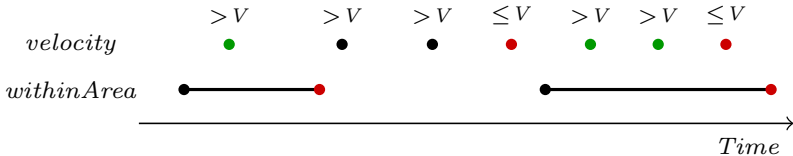
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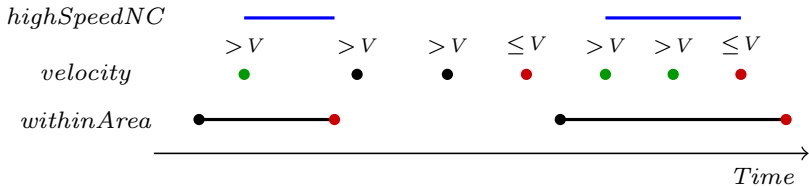
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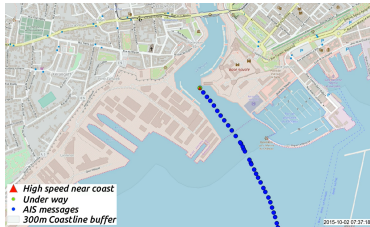


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Statically Determined Fluent: Anchored or Moored

holdsFor(*anchoredOrMoored*(*Vessel*) = true, *I*) ←
 holdsFor(*stopped*(*Vessel*) = *farFromPorts*, *I_{sf}*),
 holdsFor(*withinArea*(*Vessel*, *anchorage*) = true, *I_{wa}*),
 intersect_all([*I_{sf}*, *I_{wa}*], *I_{sa}*),
 holdsFor(*stopped*(*Vessel*) = *nearPorts*, *I_{sn}*),
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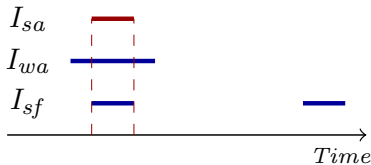
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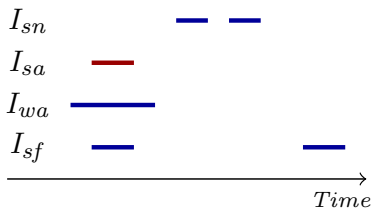
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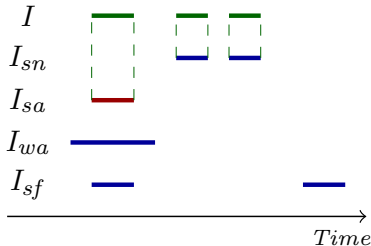
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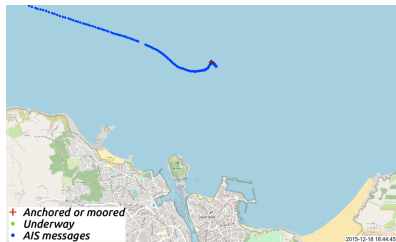
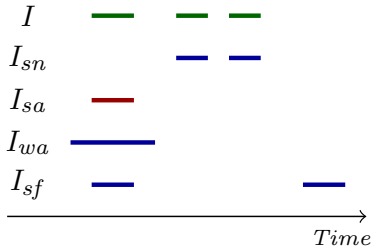
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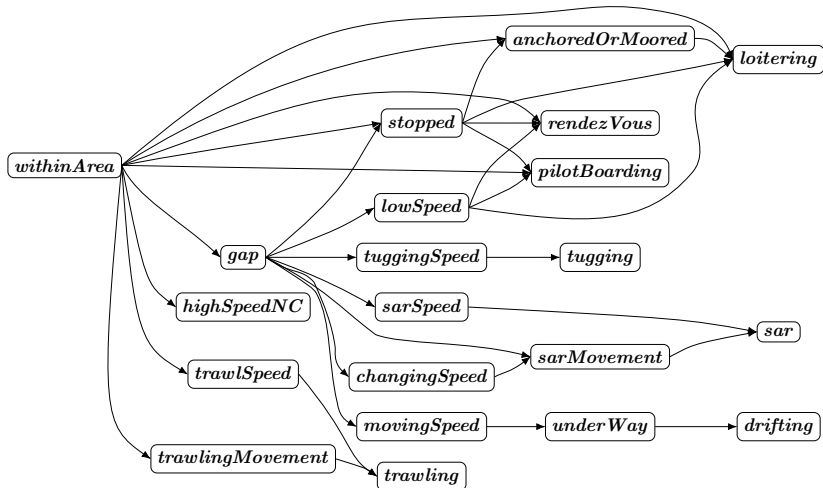


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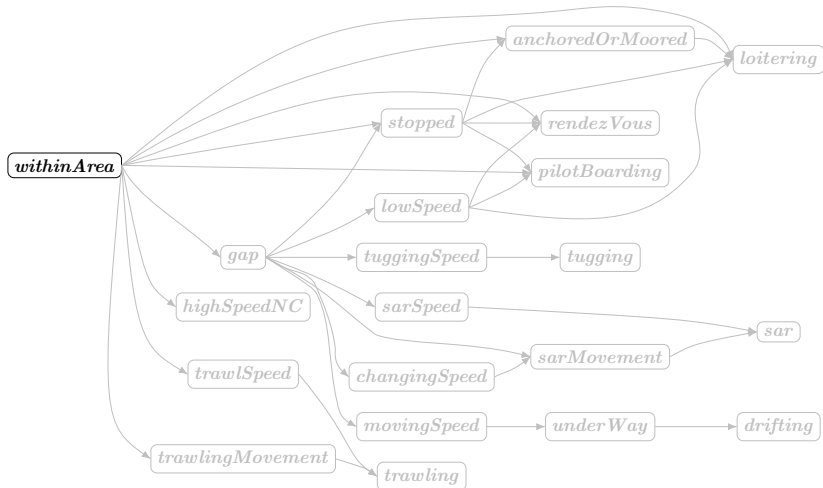


Maritime Knowledge Base



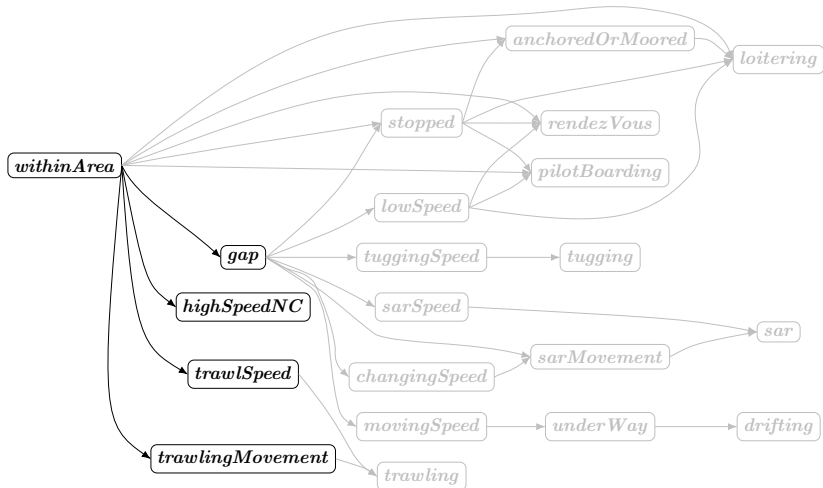
Pitsikalis E. et al., Composite Event Recognition for Maritime Monitoring. In International Conference on Distributed and Event-Based Systems (DEBS), 163–174, 2019.

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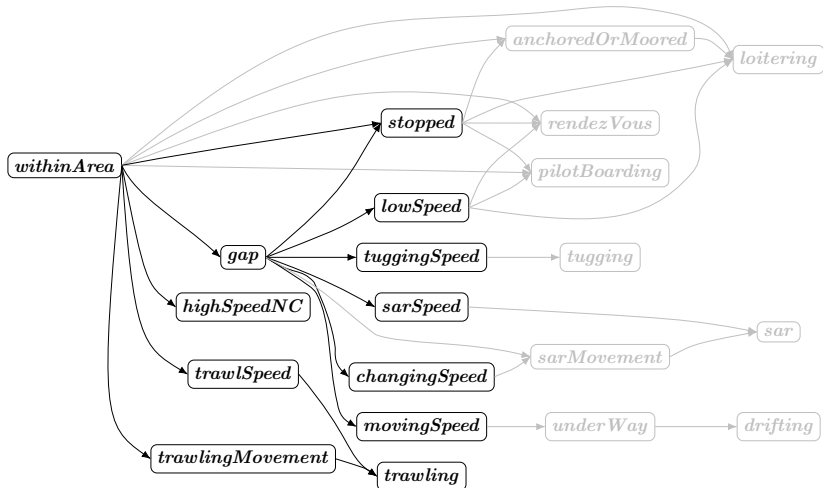
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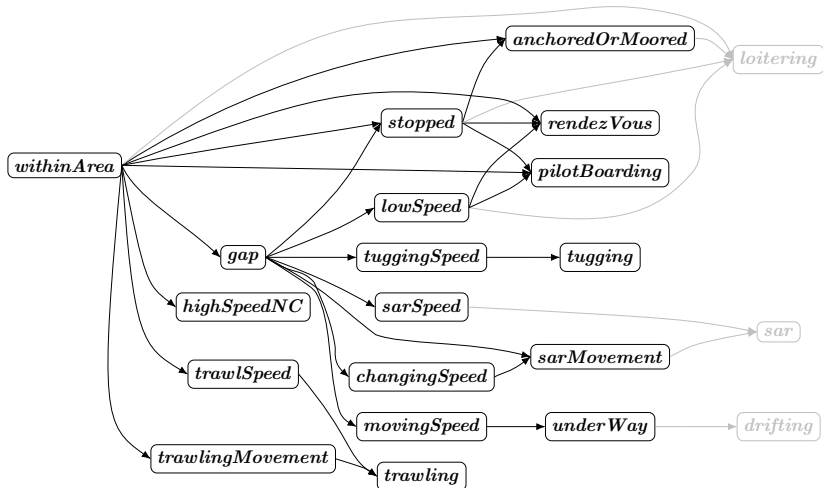
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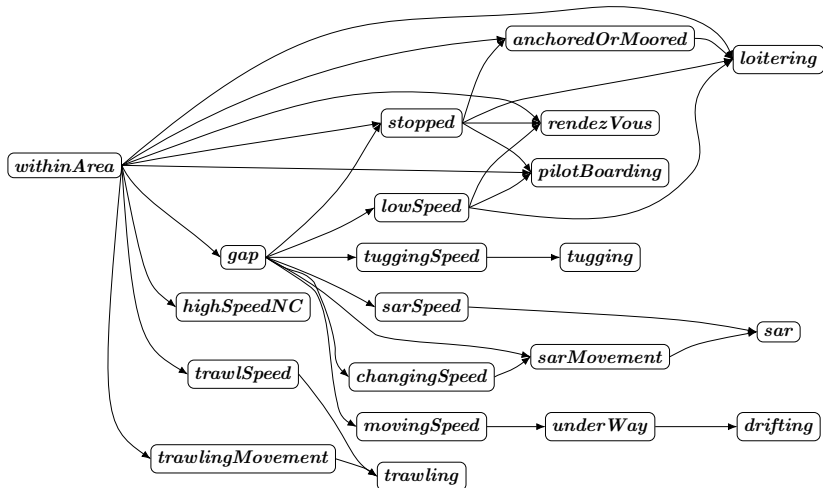
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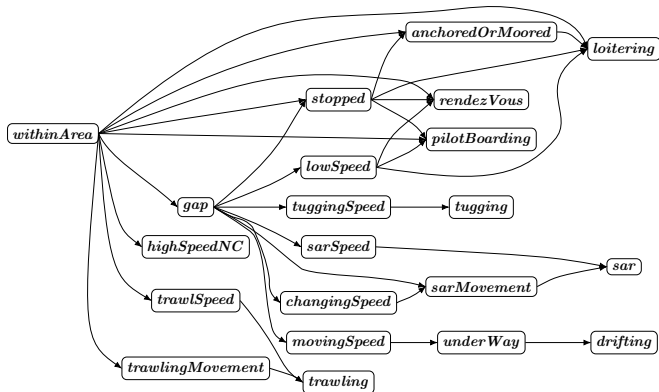
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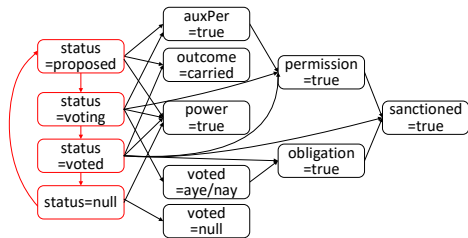
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Semantics

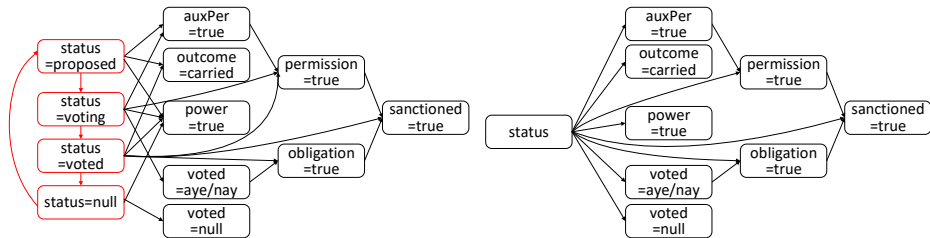
An event description of RTEC is a **locally stratified logic program**.

Cyclic Dependencies in Temporal Specifications



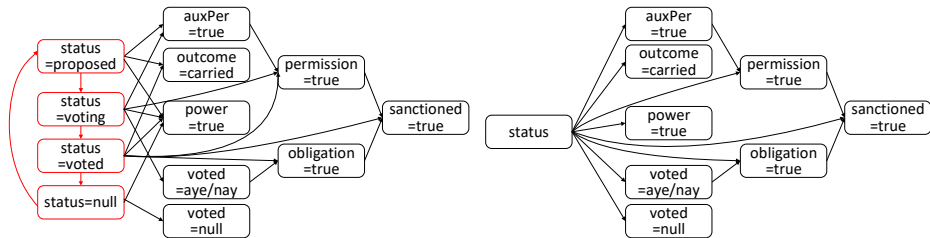
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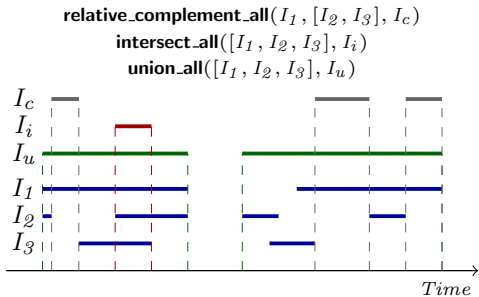
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Semantics

An event description of RTEC with cyclic dependencies is a **locally stratified logic program**.

Interval Operations & Allen Relations



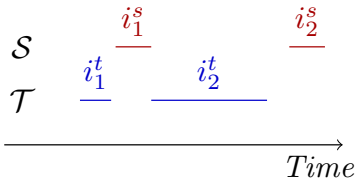
Relation	Illustration
$\text{before}(i^s, i^t)$	
$\text{meets}(i^s, i^t)$	
$\text{starts}(i^s, i^t)$	
$\text{finishes}(i^s, i^t)$	
$\text{during}(i^s, i^t)$	
$\text{overlaps}(i^s, i^t)$	
$\text{equal}(i^s, i^t)$	

RTEC with Allen Relations

holdsFor(*disappearedInArea*(*Vessel*, *AreaType*) = true, *I*) ←
holdsFor(*withinArea*(*Vessel*, *AreaType*) = true, *S*),
holdsFor(*gap*(*Vessel*) = *farFromPorts*, *T*),
allen(meets, *S*, *T*, target, *I*).

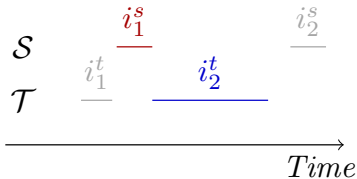
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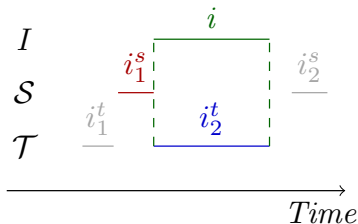
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Experimental Setup

Multi-Agent Systems: Voting & NetBill

- Compute, e.g., normative positions of agents.

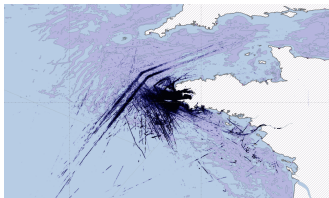
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Maritime Situational Awareness

- Recognise dangerous, illegal and suspicious vessel activity.



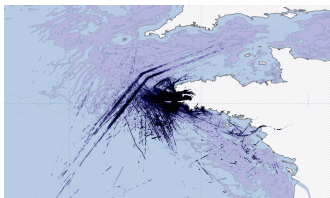
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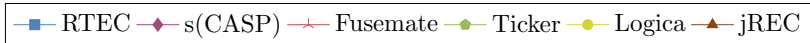
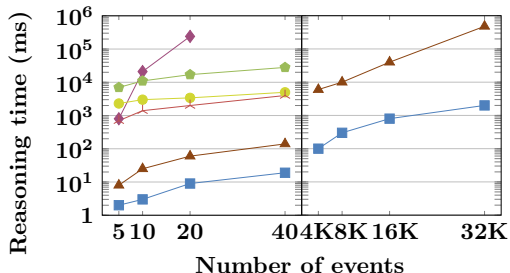
Code, Data & Temporal Specifications

<https://github.com/aartikis/RTEC>

<https://github.com/aartikis/RTEC/tree/allen>

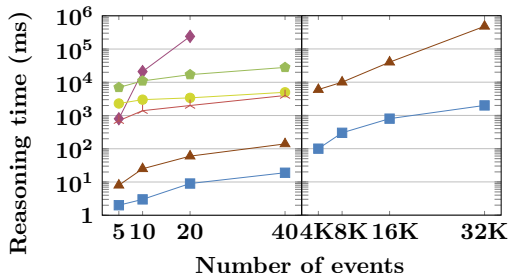
Experimental Results

NetBill: monitoring active quotes

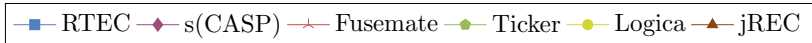
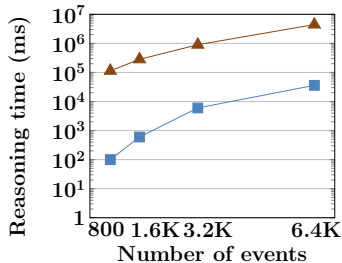


Experimental Results

NetBill: monitoring active quotes



Voting: monitoring the status of motions (cycles)



Experimental Results

Monitoring maritime activities with Allen relations

Window size		Reasoning Time (ms)		Output Intervals	
Days	Input Intervals	RTEC	D ² IA	RTEC	D ² IA
1	19K	40	410	6K	6K
2	37K	65	592	9K	9K
4	74K	99	1.1K	16K	16K
8	148K	156	1.6K	32K	31K
16	297K	285	2.7K	77K	76K

Summary & Further Work

RTEC:

- An open-source **stream reasoning** framework.
- **Locally stratified** specifications.
- Efficient treatment of **cyclic dependencies**.
- Support for **Allen relations** in event patterns.
- **Reproducible** empirical evaluation on large data streams.

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Further Work:

- Compare expressive power with **event sequencing operators**.
- Support **events with delayed effects**.

Appendix

Run-Time Event Calculus (RTEC)

Predicate	Meaning
happensAt (E, T)	Event E occurs at time T
initiatedAt ($F = V, T$)	At time T a period of time for which $F = V$ is initiated
terminatedAt ($F = V, T$)	At time T a period of time for which $F = V$ is terminated
holdsFor ($F = V, I$)	I is the list of the maximal intervals for which $F = V$ holds continuously
holdsAt ($F = V, T$)	The value of fluent F is V at time T
union_all ($[J_1, \dots, J_n], I$)	$I = (J_1 \cup \dots \cup J_n)$
intersect_all ($[J_1, \dots, J_n], I$)	$I = (J_1 \cap \dots \cap J_n)$
relative_complement_all ($I', [J_1, \dots, J_n], I$)	$I = I' \setminus (J_1 \cup \dots \cup J_n)$

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Fluent-Value Pair Computation

Definition:

initiatedAt($F = V$, T) \leftarrow
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[conditions]

...

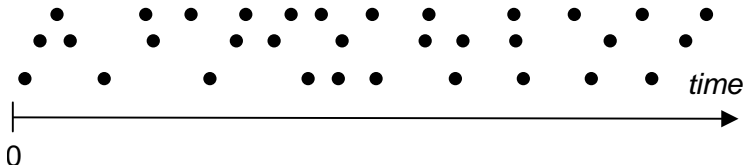
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happensAt(E_{In_i} , T),
[conditions]

terminatedAt($F = V$, T) \leftarrow
happensAt(E_{T_1} , T),
[conditions]

...

terminatedAt($F = V$, T) \leftarrow
happensAt(E_{T_j} , T),
[conditions]

Reasoning:



Fluent-Value Pair Computation

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[conditions]

...

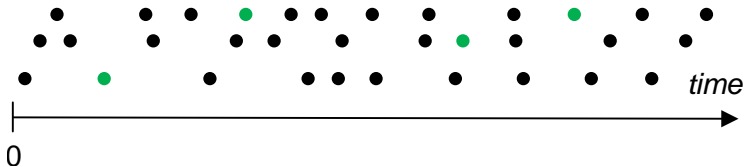
initiatedAt($F = V$, T) \leftarrow
happensAt(E_{In_i} , T),
[conditions]

terminatedAt($F = V$, T) \leftarrow
happensAt(E_{T_1} , T),
[conditions]

...

terminatedAt($F = V$, T) \leftarrow
happensAt(E_{T_j} , T),
[conditions]

Reasoning:



Fluent-Value Pair Computation

Definition:

initiatedAt($F = V$, T) \leftarrow
happensAt(E_{In_i} , T),
[conditions]

...

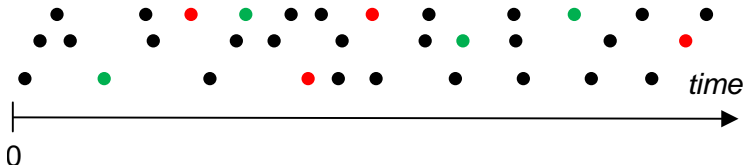
initiatedAt($F = V$, T) \leftarrow
happensAt(E_{In_i} , T),
[conditions]

terminatedAt($F = V$, T) \leftarrow
happensAt(E_{T_j} , T),
[conditions]

...

terminatedAt($F = V$, T) \leftarrow
happensAt(E_{T_j} , T),
[conditions]

Reasoning:



Fluent-Value Pair Computation

Definition:

initiatedAt($F = V, T$) \leftarrow
happensAt($E_{I_{n_1}}, T$),
[conditions]

...

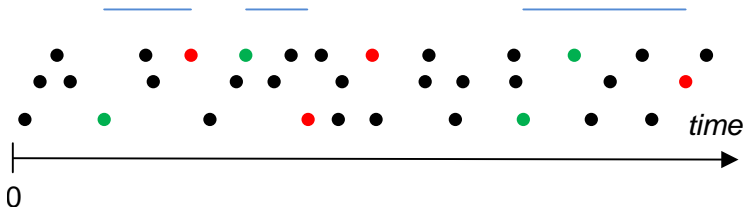
initiatedAt($F = V, T$) \leftarrow
happensAt($E_{I_{n_i}}, T$),
[conditions]

terminatedAt($F = V, T$) \leftarrow
happensAt(E_{T_1}, T),
[conditions]

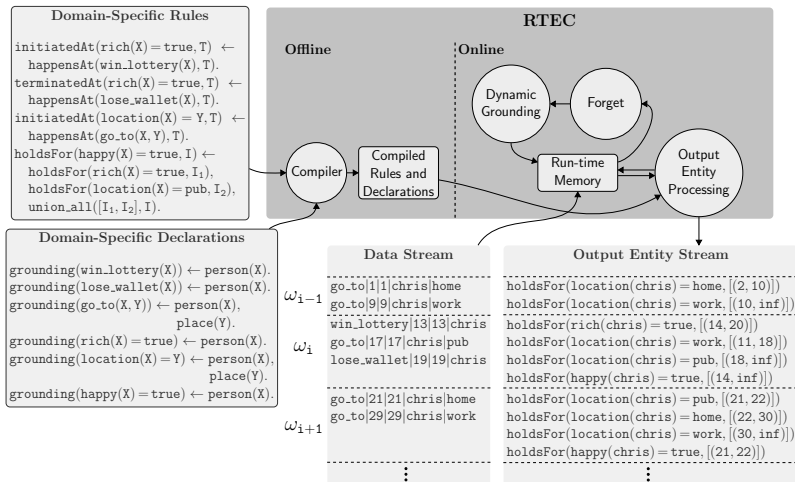
...

terminatedAt($F = V, T$) \leftarrow
happensAt(E_{T_j}, T),
[conditions]

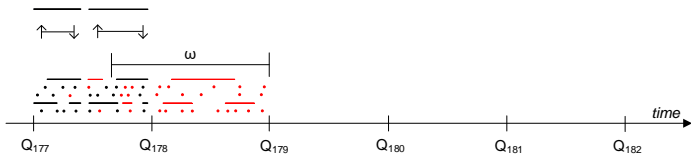
Reasoning: **holdsFor**($F = V, I$)



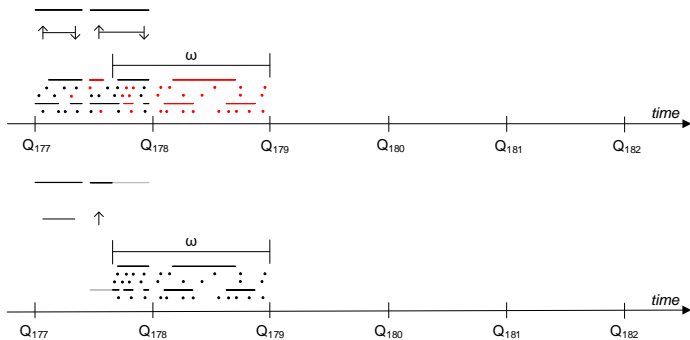
RTEC Architecture



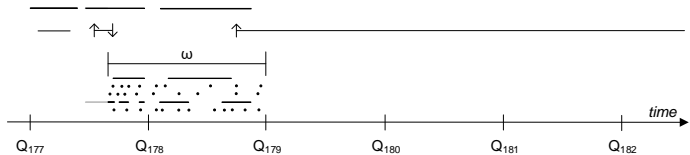
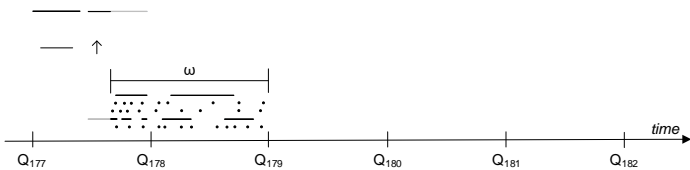
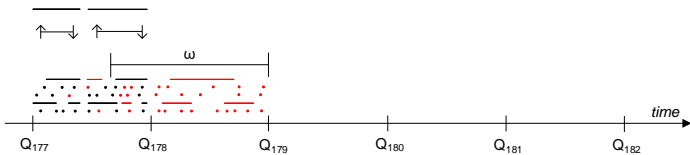
RTEC: Windowing



RTEC: Windowing



RTEC: Windowing



Cyclic Dependencies in Temporal Specifications

initiatedAt(*status*(*M*) = *proposed*, *T*) ←
happensAt(*propose*(*P*, *M*), *T*),
holdsAt(*status*(*M*) = *null*, *T*).

initiatedAt(*status*(*M*) = *voting*, *T*) ←
happensAt(*second*(*S*, *M*), *T*),
holdsAt(*status*(*M*) = *proposed*, *T*).

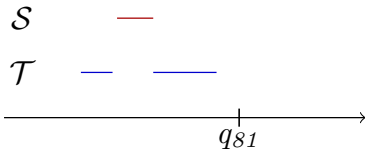
initiatedAt(*status*(*M*) = *voted*, *T*) ←
happensAt(*close_ballot*(*C*, *M*), *T*),
holdsAt(*status*(*M*) = *voting*, *T*).

initiatedAt(*status*(*M*) = *null*, *T*) ←
happensAt(*declare*(*C*, *M*, *Res*), *T*),
holdsAt(*status*(*M*) = *voted*, *T*).

RTEC_A: Windowing

holdsFor(*disappearedInArea*(*Vessel*, *AreaType*) = true, *I*) ←
holdsFor(*withinArea*(*Vessel*, *AreaType*) = true, \mathcal{S}),
holdsFor(*gap*(*Vessel*) = *farFromPorts*, \mathcal{T}),
allen(meets, \mathcal{S} , \mathcal{T} , target, *I*).

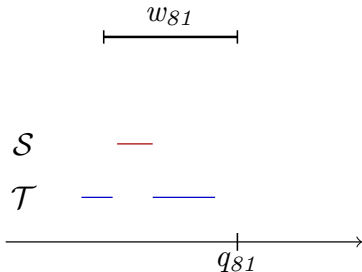
Query time: q_{81}



RTEC_A: Windowing

holdsFor(*disappearedInArea*(*Vessel*, *AreaType*) = true, *I*) ←
holdsFor(*withinArea*(*Vessel*, *AreaType*) = true, *S*),
holdsFor(*gap*(*Vessel*) = *farFromPorts*, *T*),
allen(meets, *S*, *T*, target, *I*).

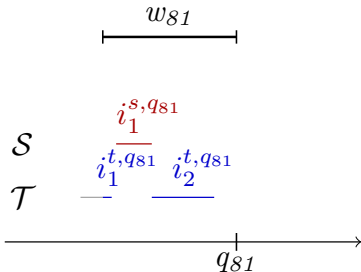
Query time: q_{81}



RTEC_A: Windowing

holdsFor(*disappearedInArea*(*Vessel*, *AreaType*) = true, *I*) ←
holdsFor(*withinArea*(*Vessel*, *AreaType*) = true, *S*),
holdsFor(*gap*(*Vessel*) = *farFromPorts*, *T*),
allen(meets, *S*, *T*, target, *I*).

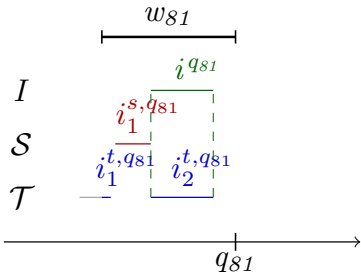
Query time: q_{81}



RTEC_A: Windowing

holdsFor(*disappearedInArea*(*Vessel*, *AreaType*) = true, *I*) ←
holdsFor(*withinArea*(*Vessel*, *AreaType*) = true, *S*),
holdsFor(*gap*(*Vessel*) = *farFromPorts*, *T*),
allen(meets, *S*, *T*, target, *I*).

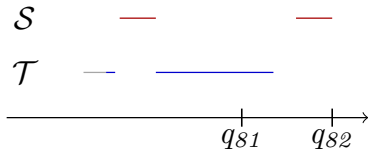
Query time: q_{81}



RTEC_A: Windowing

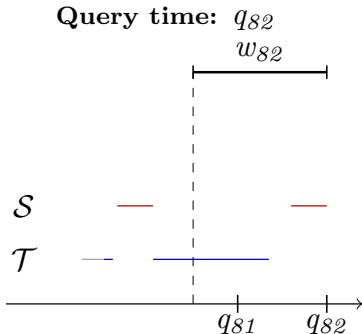
holdsFor(*disappearedInArea*(*Vessel*, *AreaType*) = true, *I*) ←
holdsFor(*withinArea*(*Vessel*, *AreaType*) = true, *S*),
holdsFor(*gap*(*Vessel*) = *farFromPorts*, *T*),
allen(meets, *S*, *T*, target, *I*).

Query time: q_{82}



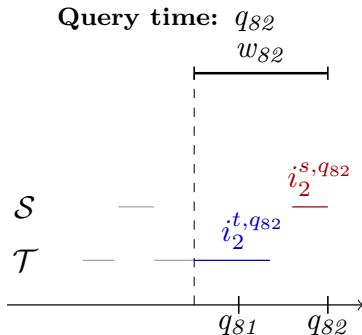
RTEC_A: Windowing

holdsFor(*disappearedInArea*(*Vessel*, *AreaType*) = true, *I*) ←
holdsFor(*withinArea*(*Vessel*, *AreaType*) = true, *S*),
holdsFor(*gap*(*Vessel*) = *farFromPorts*, *T*),
allen(meets, *S*, *T*, target, *I*).



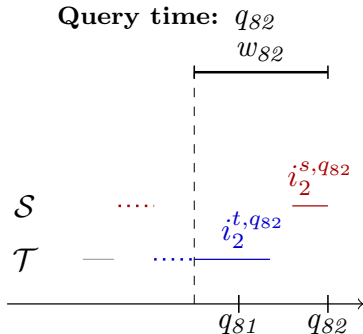
RTEC_A: Windowing

holdsFor(*disappearedInArea*(*Vessel*, *AreaType*) = true, *I*) ←
holdsFor(*withinArea*(*Vessel*, *AreaType*) = true, *S*),
holdsFor(*gap*(*Vessel*) = *farFromPorts*, *T*),
allen(meets, *S*, *T*, target, *I*).



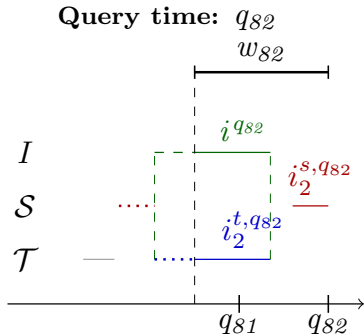
RTEC_A: Windowing

holdsFor(*disappearedInArea*(*Vessel*, *AreaType*) = true, *I*) ←
holdsFor(*withinArea*(*Vessel*, *AreaType*) = true, *S*),
holdsFor(*gap*(*Vessel*) = *farFromPorts*, *T*),
allen(meets, *S*, *T*, target, *I*).



RTEC_A: Windowing

holdsFor(*disappearedInArea*(*Vessel*, *AreaType*) = true, *I*) ←
holdsFor(*withinArea*(*Vessel*, *AreaType*) = true, *S*),
holdsFor(*gap*(*Vessel*) = *farFromPorts*, *T*),
allen(meets, *S*, *T*, target, *I*).



RTEC_A: Correctness & Complexity

Correctness of RTEC_A

RTEC_A computes all maximal intervals of a fluent defined in terms of an Allen relation, and no other interval.

RTEC_A: Correctness & Complexity

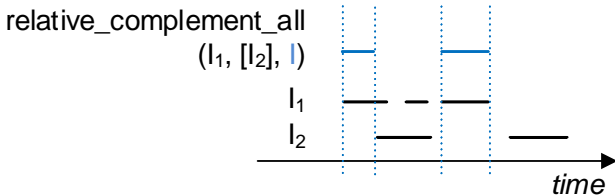
Correctness of RTEC_A

RTEC_A computes all maximal intervals of a fluent defined in terms of an Allen relation, and no other interval.

Complexity of RTEC_A

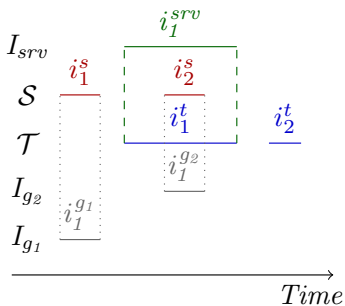
The cost of computing the maximal intervals of a fluent defined in terms of an Allen relation is $\mathcal{O}(n)$, where n is the number of input intervals.

Interval Manipulation: Relative Complement



RTEC_A: RTEC with Allen Relations

$\text{holdsFor}(\text{suspiciousRendezVous}(\text{Vessel}_1, \text{Vessel}_2) = \text{true}, I) \leftarrow$
 $\text{holdsFor}(\text{gap}(\text{Vessel}_1) = \text{farFromPorts}, I_{g_1}),$
 $\text{holdsFor}(\text{gap}(\text{Vessel}_2) = \text{farFromPorts}, I_{g_2}),$
 $\text{holdsFor}(\text{proximity}(\text{Vessel}_1, \text{Vessel}_2) = \text{true}, \mathcal{T}),$
 $\text{union_all}([I_{g_1}, I_{g_2}], \mathcal{S}),$
 $\text{allen}(\text{during}, \mathcal{S}, \mathcal{T}, \text{target}, I).$



Experimental Evaluation

Batch setting.

Batch size	Reasoning Time		
	RTEC _A	AEGLE	D ² IA
Input Intervals			
200	1	980	2K
2K	14	4K	6K
20K	154	71.5K	395K
200K	1.8K	MEM	>3.6M

Streaming setting.

Window size		Reasoning Time		Output Interval Pairs	
Days	Input Intervals	RTEC _A	D ² IA	RTEC _A	D ² IA
1	125	1	48	5K	5K
2	250	2	164	19K	18K
4	500	4	568	72K	71K
8	1K	8	1.7K	237K	236K
16	2K	15	7.8K	878K	874K